

FULL PAPER

Topological properties of sunscreens using m_{hr} -polynomial of graph

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In this work, M_{hr} -polynomial of oxybenzone, menthyl anthranilate, benzophenone-4, and dimethylamino hydroxybenzoyl hexa benzoate were established. The degree-based topological indices HDR version of Modified Zagreb topological index (HDRM*), HDR version of Modified forgotten topological index (HDRF*), and HDR version of hyper Zagreb index (HDRHM*) were obtained. Accordingly, by using the derivative of M_{hr} -polynomial of sunscreens, the HDRM*, HDRF*, and HDRHM* topological indices of sunscreens were found.

KEYWORDS

$d_{hr}(v)$ degree; HDR topological indices; M_{hr} -polynomial; oxybenzone; menthyl anthranilate; benzophenone-4; dimethylamino hydroxybenzoyl hexa benzoate.

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Introduction

A molecular graph is an undirected graph. It is denoted by $G=(V, E)$, which shows the general properties of the molecular compound, where the vertices of the shovel $|V|$ represent the number of atoms. In contrast, the edges E represent the juxtaposition relationship between those vertices that represent the atoms of the molecular compound [1]. In a molecular graph, the vertices represent atoms, and the edges represent chemical bonds, and they correspond to them. Suppose the G graph represents a chemical compound that contains a set of vertices $V(G)$, and a set of edges is $E(G)$. In that case, the degree of the vertex can be defined as the number of neighbors of the vertex in and is represented define by $d_G(v)$, which is the total number of edges associated with v [2]. Topological indices are essential relationships in modeling quantitative relationships for the structure and activity of chemical graphs [3]; for more didcestion about topological indices [7-30].

Topological indicators are fixed values in a graph by which the real values are assigned, taking the graph as a consistent median and giving similar graphs the same value. Wiener index gave the first topological index [2].

In 1947, for studying boiling points of alkanes, one of the topological indices invented at the preliminary level is the so-called Zagreb index, first provided by [4,5]. They investigated how an electron whole energy relied on the shape of molecules and became discussed. The primary Zagreb indices $M_1(G) = \sum_{uv \in E(G)} [d(u/G) + d(v/G)]$, $M_2(G) = \sum_{uv \in E(G)} [d(u/G)d(v/G)]$. [6]

DAlsinai A, at al, [1] define (1):

HDR of Zagreb index version modified of Hyper HDR Zagreb indices modified forgotten topological index of graph G by:

$$\text{HDRM}_1^*(G) = \sum_{uv \in E(G)} [d_{hr}(u/G) + d_{hr}(v/G)].$$

$$\text{HDRHM}_1^*(G) = \sum_{uv \in E(G)} [d_{hr}(u/G) + d_{hr}(v/G)]^2$$

$$\text{HDRF}^*(G) = \sum_{uv \in E(G)} [d_{hr}^2(u/G) + d_{hr}^2(v/G)].$$

And $d_{hr}(v/G) = |\{u, v \in V(G) \mid d(u/G, v/G) = \lfloor \frac{R}{2} \rfloor\}|$ And $d(u/G, v/G)$ is the distance between the nodes u and v in $V(G)$, and R is the radius of graph G .

Also, [1] are define(2): the M_{hr} polynomial for graph

G is $M_{hr}(i, j)(G)$, $i, j \geq 1$, be the $|E(G)|$ such that $\{d_{hr}(u/G); d_{hr}(v/G)\} = \{i, j\}$. Let $M_{hr}(i, j) = |M_{hr}(i, j)|$. The M_{hr} -polynomial of a graph as

$$M_{hr}(G, x, y) = \sum_{\delta_{hr} \leq i \leq j \leq \Delta_{hr}} M_{hr}(i, j) x^i y^j.$$

TABLE 1 Derivation of HDR degree-based topological Indices of graph G

Topological Indices	$f(x, y)$	Derivation From M_{hr} polynomial
$\text{HDM}_1^*(G)$	$(x+y)$	$(D_x + D_y)(M_{hr}) _{x=y=1}$
$\text{HDRHM}_1^*(G)$	$(x+y)^2$	$(D_x + D_y)^2(M_{hr}) _{x=y=1}$
$\text{HDRF}^*(G)$	$X^2 + y^2$	$(D_x^2 + D_y^2)(M_{hr}) _{x=y=1}$

Materials and methods

Our main results including computing M_{hr} -polynomial of Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate, the degree-based topological indices HDM^* , HDRF^* , and HDRHM^* obtained by using the derivative of M_{hr} -polynomial of sunscreens the HDM^* , HDRF^* , and HDRHM^* topological indices of sunscreens, are found.

Main results

This section includes two subsections computation M_{hr} -polynomial of Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate, and computation topological indices

of sunscreens (Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate).

Evaluate the M_{hr} -polynomial of Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate

In this subsection, we compute the M_{hr} -Polynomial of the sunscreens structures and we represent M_{hr} (3D) graphical using MATLAB.

Oxybenzone

Let G be a graph of oxybenzone, as shown in Figure 1. Then the graph G has 17 vertices and 17 edges.

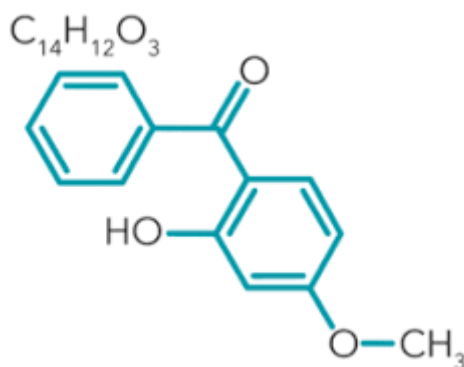


FIGURE 1 Oxybenzone graph with 17 points and 17 edges

TABLE 2 $|E|$ of Oxybenzone by $d_{hr}(v)$ degree

$M_{hr}(i,j)$	$M_{hr}(2,2)$	$M_{hr}(2,4)$	$M_{hr}(2,5)$	$M_{hr}(3,4)$	$M_{hr}(3,5)$	$M_{hr}(4,5)$	$M_{hr}(3,3)$	$M_{hr}(2,3)$	$M_{hr}(1,2)$
no.edge	3	1	1	2	3	1	2	2	2

Theorem 1. Let G be a graph of oxybenzone.

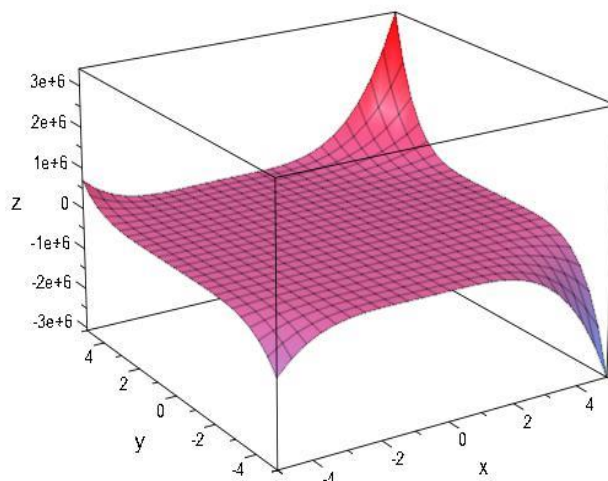
Then

$$M_{hr}(G, x, y) = 2xy^2 + 3x^2x^2 + x^2y^4 + x^2y^5 + 2x^3y^4 + 3x^3y^5 + x^4y^5 + 2x^3y^3 + 2x^2y^3.$$

Proof. Let G a graph of Oxybenzone as in Figure 1. Then by using Table 2 and Definition 2, we have:

$$\begin{aligned} M_{hr}(G, x, y) &= \sum_{\delta_{hr} \leq i \leq j \leq \Delta_{hr}} M_{hr}(i, j) x^i y^j \\ &= M_{hr}(1,2) x y^2 \\ &\quad + M_{hr}(2,2) x^2 y^2 \\ &\quad + M_{hr}(2,4) x^2 y^4 \\ &\quad + M_{hr}(2,5) x^2 y^5 \\ &\quad + M_{hr}(3,4) x^3 x^4 \\ &\quad + M_{hr}(3,5) x^3 y^5 \\ &\quad + M_{hr}(4,5) x^4 y^5 \\ &\quad + M_{hr}(3,3) x^3 y^3 \\ &\quad + M_{hr}(2,3) x^2 y^3 \end{aligned}$$

$$= 2xy^2 + 3x^2y^2 + x^2y^4 + x^2y^5 + 2x^3y^4 + 3x^3y^5 + x^4y^5 + 2x^3y^3 + 2x^2y^3.$$

**FIGURE 2** M_{hr} –polynomial of oxybenzon

Menthyl anthranilate

Let G be a graph of Menthyl Anthranilate, as shown in Figure 3. The graph G contain 18 vertices and 19 edges.

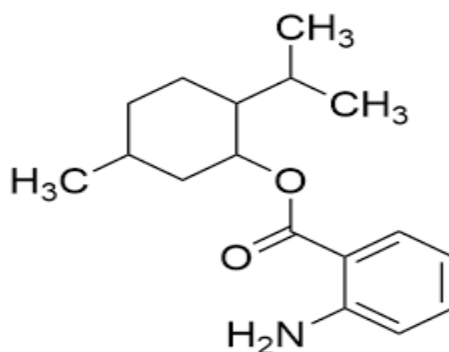
**FIGURE 3** The graph of menthyl anthranilate with 19 points and 20 edge

TABLE 3 The $|E(G)|$ of menthyl anthranilate using $d_{hr}(u)$ degree

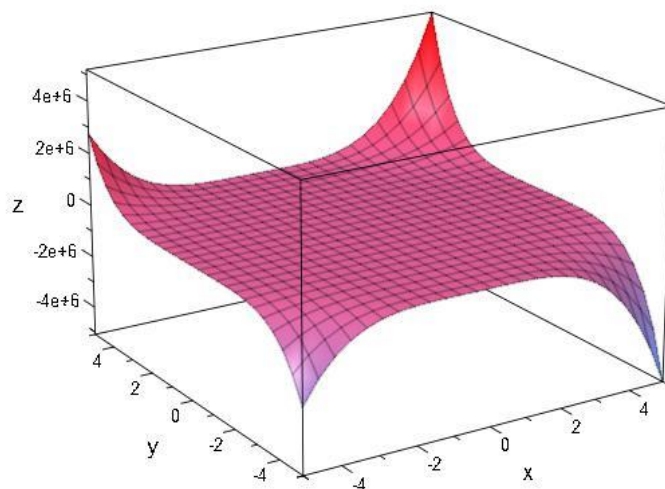
$M_{hr}(i, j)$	$M_{hr}(2, 2)$	$M_{hr}(2, 3)$	$M_{hr}(3, 3)$	$M_{hr}(3, 5)$	$M_{hr}(5, 4)$	$M_{hr}(2, 4)$
no.edge	5	4	3	3	3	2

Theorem 2. Let G be a graph of menthyl anthranilate. Then

$$M_{hr}(G, x, y) = 5x^2y^2 + 4x^2y^3 + 3x^2y^4 + 3x^3y^3 + 3x^3y^5 + 2x^4y^5$$

Proof. Let G be a graph of Menthyl Anthranilate as in Figure3. Then by using Table 3 and Definition 2, we have

$$\begin{aligned} M_{hr}(G, x, y) &= \sum_{\delta_{hr} \leq i \leq j \leq \Delta_{hr}} M_{hr}(i, j) x^i y^j = \\ &M_{hr}(2, 2) x^2 y^2 + \\ &M_{hr}(2, 3) x^2 y^3 + M_{hr}(2, 4) x^2 y^4 + \\ &M_{hr}(3, 3) x^3 y^3 + M_{hr}(3, 5) x^3 y^5 + \\ &M_{hr}(4, 5) x^4 y^5 \\ &= 5x^2 y^2 + 4x^2 y^3 + 3x^2 y^4 + 3x^3 y^3 + 3x^3 y^5 \\ &\quad + 2x^4 y^5. \end{aligned}$$

**FIGURE 4** M_{hr} –polynomial of menthyl anthranilate

Benzophenone-4

Let G be a graph of Benzophenone-4, as shown in Figure 5. Then the graph G contain 21 points and 22 edges and

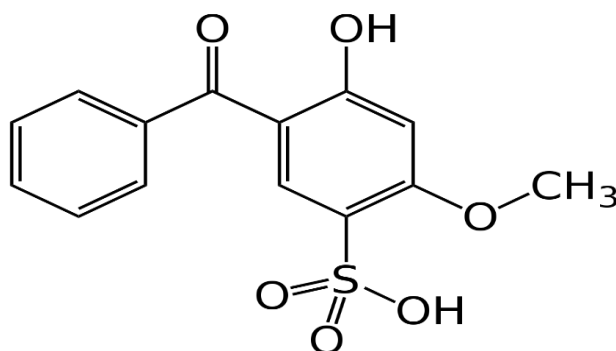
**FIGURE 5** The graph of benzophenone-4 contains 22vertices and 21 edges

TABLE 4 The number of edges of benzophenone-4 using $d_{hr}(v)$ degree

$M_{hr}(i, j)$	$M_{hr}(2, 3)$	$M_{hr}(3, 3)$	$M_{hr}(3, 8)$	$M_{hr}(3, 5)$	$M_{hr}(4, 8)$	$M_{hr}(4, 4)$
no.edge	6	3	1	3	1	2
$M_{hr}(i, j)$	$M_{hr}(4, 5)$	$M_{hr}(3, 4)$	$M_{hr}(1, 2)$			
no.edge	3	1	2			

Theorem 3. Let G be the graph of benzophenone-4. Then

$$M_{hr}(G, x, y) = 6x^2y^3 + 3x^3y^3 + x^3y^8 + 3x^3y^5 + x^4y^8 + 2x^4y^4 + 3x^4y^5 + x^3y^4 + 2xy^2$$

Proof. Let G be the graph of Benzophenone-4, as seen in Figure 5. Then by using Table 4 and Definition 2, we have:

$$\begin{aligned} M_{hr}(G, x, y) &= \sum_{\delta_{hr} \leq i \leq j \leq \Delta_{hr}} M_{hr}(i, j) x^i y^j \\ &= M_{hr}(1, 2) x y^2 \\ &\quad + M_{hr}(2, 3) x^2 y^3 \\ &\quad + M_{hr}(2, 2) x^2 y^2 \\ &\quad + M_{hr}(3, 3) x^3 y^3 \\ &\quad + M_{hr}(3, 8) x^3 y^8 \\ &\quad + M_{hr}(3, 5) x^3 y^5 \\ &\quad + M_{hr}(4, 8) x^4 y^8 \\ &\quad + M_{hr}(4, 4) x^4 y^4 \\ &\quad + M_{hr}(4, 5) x^4 y^5 \\ &\quad + M_{hr}(3, 4) x^3 y^4 \\ &= 6x^2y^3 + 3x^3y^3 + x^3y^8 + 3x^3y^5 + x^4y^8 \\ &\quad + 2x^4y^4 + 3x^4y^5 + x^3y^4 \\ &\quad + 2xy^2 \end{aligned}$$

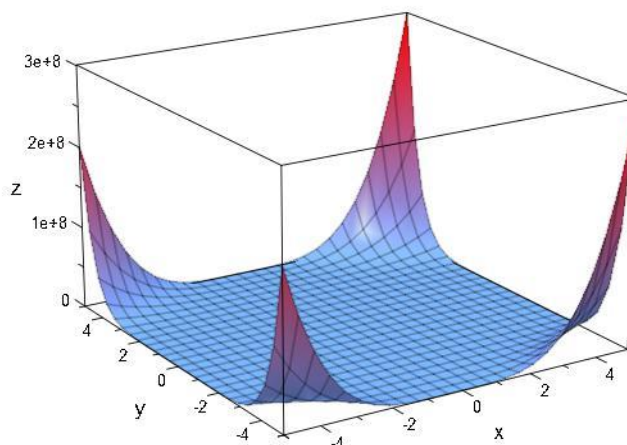


FIGURE 6 M_{hr} –polynomial of benzophenone-4

Dimethylamino hydroxybenzoyl hexa benzoate

Let G be the graph of Dimethylamino hydroxybenzoyl hexa benzoate, as shown in

Figure 7. The graph G contains 21 points and 22 edges.

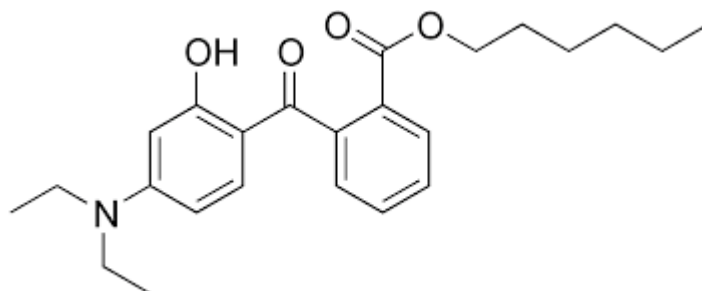


FIGURE 7 The graph of dimethylamino hydroxybenzoyl hexa benzoate with 27 vertices and 29 edges

TABLE 5 The number of edges of Dimethylamino hydroxybenzoyl hexa benzoate, using $d_{hr}(v)$ degree

$M_{hr}(i, j)$	$Mhr(1, 1)$	$Mhr(2, 2)$	$Mhr(2, 4)$	$Mhr(4, 4)$	$Mhr(3, 4)$	$Mhr(3, 3)$
no.edge	4	4	2	1	4	3
$M_{hr}(i, j)$	$Mhr(2, 3)$	$Mhr(2, 5)$	$Mhr(5, 5)$	$Mhr(1, 2)$		
no.edge	2	3	2	4		

Theorem 4. Let G be a molecular graph of Dimethylamino hydroxybenzoyl hexa benzoate, then

$$M_{hr}(G, x, y) = 4xy + 4xy^2 + 4x^2y^2 + 2x^2y^4 + x^4y^4 + 4x^3y^4 + 3x^3y^3 + 2x^2y^3 + 3x^2y^5 + 3x^5y^5$$

Proof. Let G a molecular graph of Dimethylamino hydroxybenzoyl hexa benzoate, as seen in Figure 7. Then by using Table 5 and Definition 2, we have

$$\begin{aligned}
 M_{hr}(G, x, y) &= \sum_{\delta_{hr} \leq i \leq j \leq \Delta_{hr}} M_{hr}(i, j) x^i y^j \\
 &= Mhr(1, 1)xy \\
 &\quad + Mhr(1, 2)x^2y^2 \\
 &\quad + Mhr(2, 2)x^2y^2 \\
 &\quad + Mhr(2, 4)x^2y^4 \\
 &\quad + M_{hr}(4, 4)x^4y^4 \\
 &\quad + M_{hr}(3, 4)x^3y^4 \\
 &\quad + M_{hr}(3, 3)x^3y^3 \\
 &\quad + M_{hr}(2, 3)x^2y^3 \\
 &\quad + M_{hr}(2, 5)x^2y^5 \\
 &\quad + M_{hr}(5, 5)x^5y^5 \\
 &= 4xy + 4xy^2 + 4x^2y^2 + 2x^2y^4 + x^4y^4 \\
 &\quad + 4x^3y^4 + 3x^3y^3 + 2x^2y^3 \\
 &\quad + 3x^2y^5 + 3x^5y^5
 \end{aligned}$$

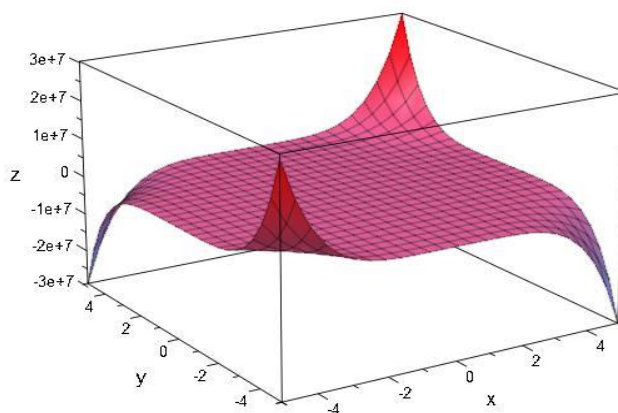


FIGURE 8 M_{hr} –polynomial of dimethylamino hydroxybenzoyl hexa benzoate

Computation HDR topological indices of sunscreens (Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate)

In this subsection, we computed HDR indices of Modified Zagreb topological index (HDRM*), (HDRF*), and (HDRHM*) by using the derivative of Mhr- polynomial of sunscreens

Theorem 5. Let G be the graph of Oxybenzone, and

$$M_{hr}(G, x, y) = 2xy^2 + 3x^2y^2 + x^2y^4 + x^2y^5 + 2x^3y^4 + 3x^3y^5 + x^4y^5 + 2x^3y^3 + 2x^2y^3. \text{ Then.}$$

$$\text{HDRM}_1^*(G) = 102.$$

$$\text{HDRF}^*(G) = 383.$$

$$\text{HDRHM}_1^*(G) = 408.$$

Proof. Let $M_{hr}(G, x, y) = f(x, y) = 2xy^2 + 3x^2y^2 + x^2y^4 + x^2y^5 + 2x^3y^4 + 3x^3y^5 + x^4y^5 + 2x^3y^3 + 2x^2y^3$. Then we have,

$$(D_x + D_y)f(x, y) = 11x^4y^5 + 24x^3y^5 + 14x^3y^4 + 12x^3y^3 + 7x^2y^5 + 6x^2y^4 + 10x^2y^3 + 12x^2y^2 + 6xy^2.$$

$$(D_x^2 + D_y^2)f(x, y) = 41x^4y^5 + 102x^3y^5 + 50x^3y^4 + 36x^3y^3 + 29x^2y^5 + 20x^2y^4 + 26x^2y^3 + 24x^2y^2 + 10xy^2.$$

$$(D_x + D_y)^2f(x, y) = 51x^4y^5 + 114x^3y^5 + 62x^3y^4 + 48x^3y^3 + 27x^2y^5 + 22x^2y^4 + 34x^2y^3 + 36x^2y^2 + 14xy^2.$$

Using Table 1, we find the outcome. ■

Theorem 6. Let G be a molecular graph of Menthyl Anthranilate, and

$$M_{hr}(G, x, y) = 5x^2y^2 + 4x^2y^3 + 3x^2y^4 + 3x^3y^3 + 3x^3y^5 + 2x^4y^5. \text{ Then}$$

$$\text{HDRM}_1^*(G) = 118.$$

$$\text{HDRF}^*(G) = 390$$

$$\text{HDRHM}_1^*(G) = 750.$$

Proof. Let $M_{hr}(G, x, y) = f(x, y) = 5x^2y^2 + 4x^2y^3 + 3x^3y^3 + 3x^3y^5 + 2x^4y^5$.

Then we have,

$$(D_x + D_y)f(x, y) = 20x^2y^2 + 20x^2y^3 + 18x^2y^4 + 18x^3y^3 + 24x^3y^5 + 18x^4y^5.$$

$$(D_x^2 + D_y^2)f(x, y) = 41x^4y^5 + 102x^3y^5 + 50x^3y^4 + 36x^3y^3 + 29x^2y^5 + 20x^2y^4 + 26x^2y^3 + 24x^2y^2 + 10xy^2.$$

$$(D_x + D_y)^2f(x, y) = 80x^2y^2 + 100x^2y^3 + 108x^2y^4 + 108x^3y^3 + 192x^3y^5 + 162x^4y^5$$

Using Table 1, we find the outcome. ■

Theorem 7. Let G be a molecular graph of Benzophenone-4, and

$$M_{hr}(G, x, y) = 6x^2y^3 + 3x^3y^3 + x^3y^8 + 3x^3y^5 + x^4y^8 + 2x^4y^4 + 3x^4y^5 + x^3y^4 + 2xy^2. \text{ Then}$$

$$\text{HDRM}_1^*(G) = 148$$

$$\text{HDRF}^*(G) = 390$$

$$\text{HDRHM}_1^*(G) = 1137.$$

Proof. Let $M_{hr}(G, x, y) = f(x, y) = 6x^2y^3 + 3x^3y^3 + x^3y^8 + 3x^3y^5 + x^4y^8 + 2x^4y^4 + 3x^4y^5 + x^3y^4 + 2xy^2$. Then

Then we have,

$$(D_x + D_y)f(x, y) = 30x^2y^3 + 15x^3y^3 + 11x^3y^8 + 24x^3y^5 + 12x^4y^8 + 16x^4y^4 + 27x^4y^5 + 7x^3y^4 + 6xy^2. \text{ Then}$$

$$\begin{aligned} (D_x^2 + D_y^2)f(x, y) &= 78x^2y^3 + 45x^3y^3 \\ &+ 73x^3y^8 + 102x^3y^5 \\ &+ 80x^4y^8 + 64x^4y^4 \\ &+ 168x^4y^5 + 25x^3y^4 \\ &+ 10xy^2 \end{aligned}$$

$$\begin{aligned} (D_x + D_y)^2f(x, y) &= 150x^2y^3 + 99x^3y^3 \\ &+ 121x^3y^8 + 192x^3y^5 \\ &+ 128x^4y^8 + 128x^4y^4 \\ &+ 288x^4y^5 + 49x^3y^4 \\ &+ 18xy^2 \end{aligned}$$

Using Table 1, we find the outcome. ■

Theorem 8. Let G be a molecular graph of Dimethylamino hydroxybenzoyl hexa benzoate, and

$M_{hr}(G, x, y) = 4xy + 4xy^2 + 4x^2y^2 + 2x^2y^4 + x^4y^4 + 4x^3y^4 + 3x^3y^3 + 2x^2y^3 + 3x^2y^5 + 3x^5y^5$. Then

$$\text{HDRM}_1^*(G) = 163.$$

$$\text{HDRF}^*(G) = 549.$$

$$\text{HDRHM}_1^*(G) = 1055.$$

Proof. Let $M_{hr}(G, x, y) = f(x, y) = 4xy + 4xy^2 + 4x^2y^2 + 2x^2y^4 + x^4y^4 + 4x^3y^4 + 3x^3y^3 + 2x^2y^3 + 3x^2y^5 + 3x^5y^5$. Then

Then we have,

$$(D_x + D_y)f(x, y) = 8xy + 12xy^2 + 16x^2y^2 + 12x^2y^4 + 8x^4y^4 + 28x^3y^4 + 18x^3y^3 + 10x^2y^3 + 21x^2y^5 + 30x^5y^5.$$
 Then

$$\begin{aligned} (D_x^2 + D_y^2)f(x, y) &= 8xy + 20xy^2 + 32x^2y^2 \\ &+ 40x^2y^4 + 32x^4y^4 \\ &+ 100x^3y^4 + 54x^3y^3 \\ &+ 26x^2y^3 + 87x^2y^5 \\ &+ 150x^5y^5 \end{aligned}$$

$$(D_x + D_y)^2f(x, y) = 16xy + 36xy^2 + 64x^2y^2 + 72x^2y^4 + 64x^4y^4 + 198x^3y^4 + 108x^3y^3 + 50x^2y^3 + 147x^2y^5 + 300x^5y^5. \blacksquare$$

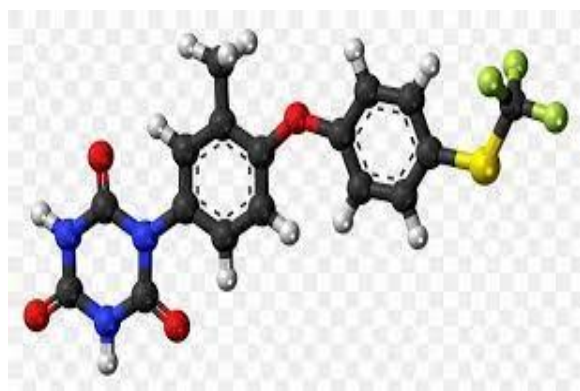


FIGURE 6 The structure of Benzophenone-4

Conclusion

We found Mhr- polynomial of Oxybenzone, Menthyl Anthranilate, Benzophenone-4, and Dimethylamino hydroxybenzoyl hexa benzoate, the degree-based topological indices HDRM*, HDRF*, HDRHM* obtained. By using the derivative of Mhr- polynomial of sunscreens the HDRM*, HDRF*, and HDRHM*

topological indices of sunscreens, were found. The results of the HDRM*, HDRF*, and HDRHM* of sunscreens are better than the leap indices and Zagreb Indices.

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